

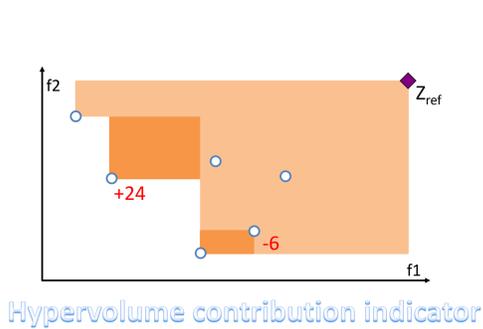
Experiments on Path Relinking Methods for bi-objective FlowShop problem

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Hybrid Path Relinking algorithm (HPR)

Cooperation of 2 algorithms:

- Hypervolume-Based Multi-Objective Local Search (HBMOLS)
- Multi-Objective Path Relinking (MOPR)



HBMOLS

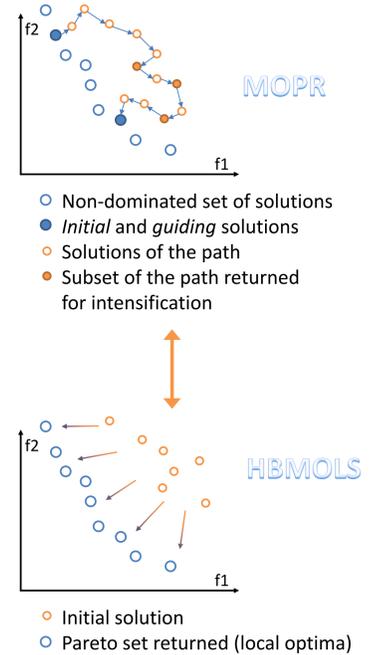
Repeat

- Step 1: assign a fitness value to each solution in the population according to the hypervolume contribution indicator
- Step 2: generate a new solution from the neighborhood of a solution of the population
- Step 3: evaluating the new solution using the hypervolume contribution indicator
- Step 4: delete the solution with the worst fitness value from the population

Until all neighborhood explored without any improvement
Return the population

MOPR

- Step 1: randomly choose an initial and a guiding solution from a Pareto set approximation
- Step 2: generate a path (set of solutions) linking the initial solution to the guiding solution
- Step 3: return a subset of the path (for intensification)



Path Relinking Strategies

Initial and guiding solution selection

- Random
- Similar
- Different

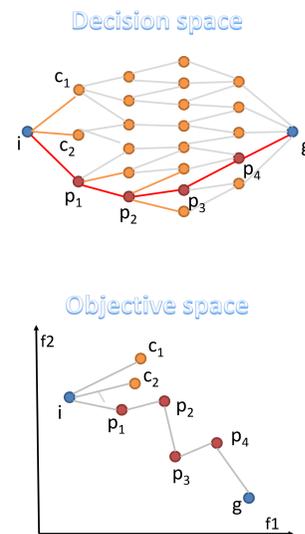
Path generation strategies

- Without comparison
 - First/Last : First/Last move reducing the distance to the guiding solution
 - Random: Random candidate move
- With comparison : Generate and evaluate all candidate moves
 - Pareto-Based: select randomly a *non-dominated* solution
 - Hypervolume-Based: select the solution with the largest hypervolume

Subset selection

To be returned for intensification

- Without comparison
 - All: The entire path
 - Middle: The solution located in the « center » of the path
 - k-middle: A set of solutions located in the middle of the path
- With comparison
 - Best: The set of non-dominated solutions of the path



i: Initial solution
g: Guiding solution
○ — ○ : Neighbors
c₁, c₂, p₁: First candidates for path generation
p_i: Path candidates to be returned

Path generation: iteratively build a path by choosing among candidates c_i.

- First: c₁
- Last: p₁
- Random: p₁ or p₂ or p₃
- Pareto: p₁
- Hypervolume: p₁

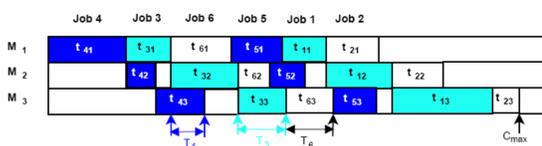
Subset selection:

- All: p₁, p₂, p₃ and p₄
- Middle: p₂ or p₃
- k-middle: p₂ and p₃
- Best: p₁ and p₃

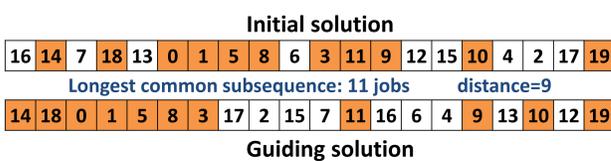
Experiments

Permutation biobjective flowshop

- N jobs to schedule on M machines
- Jobs and machines are critical resources
- Jobs are treated on a defined order of machines
- 2 objectives functions : Maximal completion time (C_{max}) and Total tardiness (T_{sum})



Insertion operator: minimal path generation using the corresponding distance measure



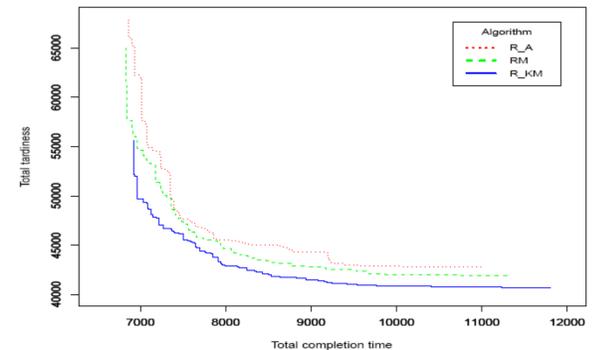
Results

Significant differences obtained between subset selection strategies →

PR_A: All
PR_B: Best
PR_M: Middle
PR_KM: k-middle
RM: random mutations
CO: crossover operator

| Instance | Algorithm | | | | | |
|-----------------|-----------|----------|----------|-----------------|-----------------|-----------------|
| | PR_A | PR_B | PR_M | PR_KM | RM | CO |
| 20_05_01_ta001 | 0.050496 | 0.076627 | 0.093801 | 0.067028 | 0.000260 | 0.005152 |
| 20_10_01_ta011 | 0.023355 | 0.055498 | 0.048349 | 0.034595 | 0.000739 | 0.027353 |
| 20_15_01 | 0.032433 | 0.073174 | 0.070448 | 0.037654 | 0.002330 | 0.037131 |
| 20_20_01_ta021 | 0.009737 | 0.034508 | 0.024761 | 0.010079 | 0.000077 | 0.044826 |
| 30_05_01 | 0.049260 | 0.081154 | 0.099705 | 0.040607 | 0.011844 | 0.062030 |
| 30_10_01 | 0.100098 | 0.200979 | 0.176367 | 0.088794 | 0.041814 | 0.116553 |
| 30_15_01 | 0.052479 | 0.096203 | 0.105293 | 0.048227 | 0.028186 | 0.054050 |
| 30_20_01 | 0.048423 | 0.064844 | 0.071167 | 0.040580 | 0.035835 | 0.051028 |
| 50_05_01_ta031 | 0.031220 | 0.083466 | 0.090345 | 0.022628 | 0.041017 | 0.056559 |
| 50_10_01_ta041 | 0.103891 | 0.149919 | 0.132192 | 0.079505 | 0.089703 | 0.116051 |
| 50_15_01 | 0.131563 | 0.173639 | 0.156972 | 0.091552 | 0.114880 | 0.131505 |
| 50_20_01_ta051 | 0.129671 | 0.176523 | 0.146388 | 0.093540 | 0.117150 | 0.141695 |
| 70_05_01 | 0.110650 | 0.191452 | 0.152058 | 0.096111 | 0.084047 | 0.146741 |
| 70_10_01 | 0.131195 | 0.177933 | 0.157369 | 0.119054 | 0.146445 | 0.172327 |
| 70_15_01 | 0.149831 | 0.174514 | 0.164179 | 0.134607 | 0.156965 | 0.178769 |
| 70_20_01 | 0.139377 | 0.183869 | 0.147617 | 0.102067 | 0.135491 | 0.137697 |
| 100_05_01_ta061 | 0.199309 | 0.359023 | 0.236139 | 0.157834 | 0.169815 | 0.175162 |
| 100_10_01_ta071 | 0.093883 | 0.121682 | 0.104086 | 0.071063 | 0.080287 | 0.086577 |
| 100_15_01 | 0.187296 | 0.205879 | 0.175943 | 0.128876 | 0.163312 | 0.174849 |
| 100_20_01_ta081 | 0.205930 | 0.220908 | 0.187275 | 0.131843 | 0.137246 | 0.180406 |

Empirical attainment function
Instance 100_15_01 (100 jobs, 15 machines)



Conclusions and Perspectives

Conclusion

- Proposition of a generic approach combining path-relinking and local search in a MO context
- The use of path relinking offer a good alternative to RM and CO to iterate local searches
- No significant observation concerning the path generation method
- The solutions located in the middle of the path should be selected for intensification (k-middle)

Perspectives

- Application to other multi-objective optimization problems
- Evaluate methods selecting the initial and guiding solutions
- Toward advanced path-relinking algorithms (path between more than two solutions, generate several paths simultaneously...)