

Centre for
Advanced
Composite
Materials

Applying Bi-level Multi-Objective Evolutionary Algorithms for Optimizing Composites Manufacturing Processes

Abhishek Gupta, Piaras Kelly, Matthias Ehrgott,
Simon Bickerton

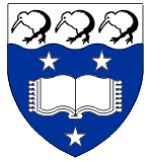
Centre for Advanced Composite Materials
&
The Department of Engineering Science, University
of Auckland

BMW, Landshut, Germany





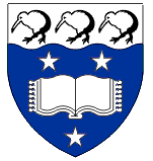
Outline



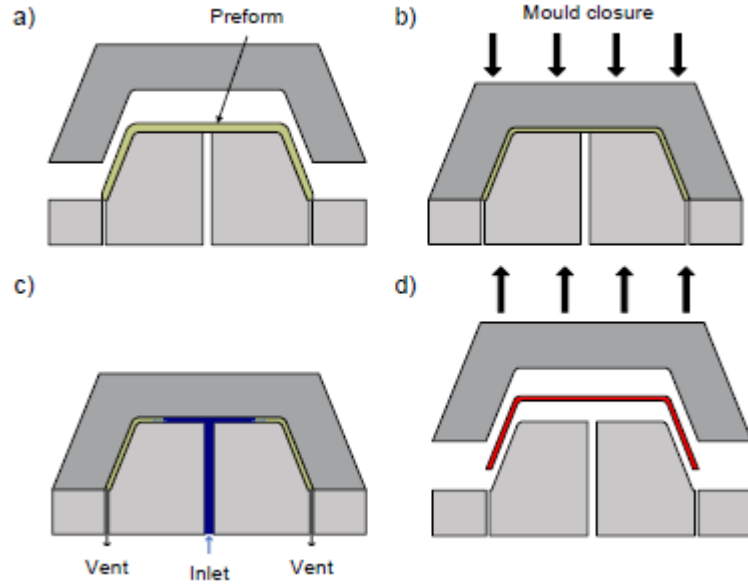
- **Introduction to Composite Manufacturing processes – Resin Transfer Moulding (RTM) and Compression RTM (CRTM) .**
- **Objectives under consideration.**
- **Non-intuitive consequences of certain process variables.**
- **Structure of the manufacturing cycle optimization problem.**
- **Solution approach.**
- **Results from a test case.**



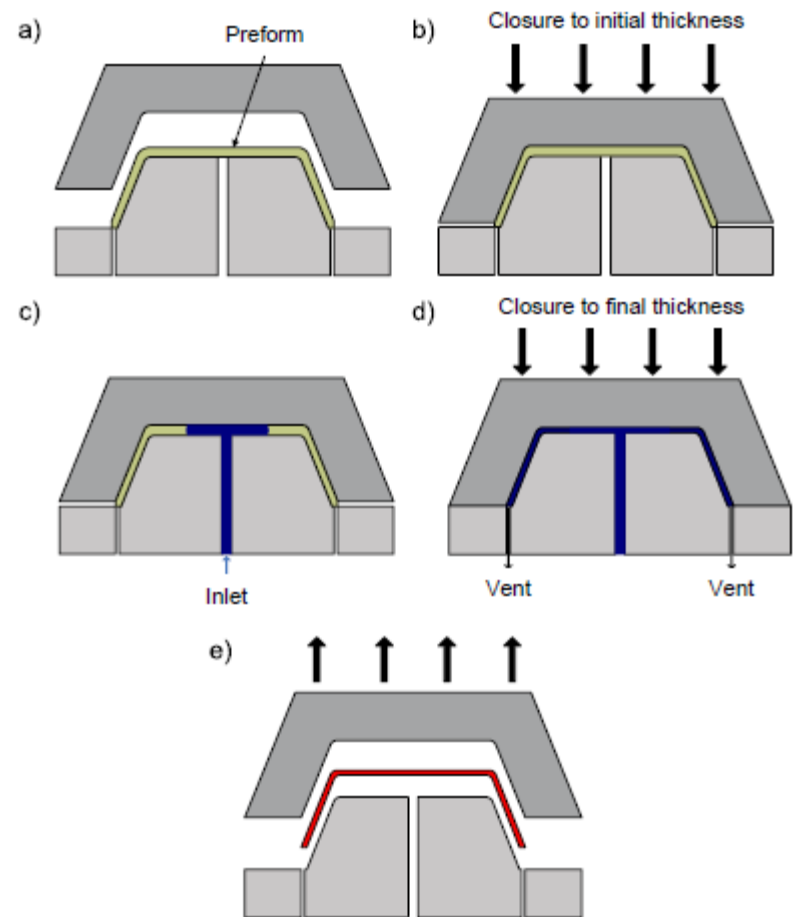
RTM and CRTM



RTM

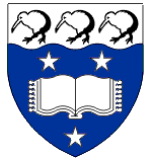


CRTM





Objectives under consideration



Filling phase:

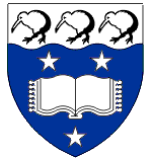
- **Fill time - Minimize**
- **Tooling forces - Minimize**

Curing (Solidification) phase:

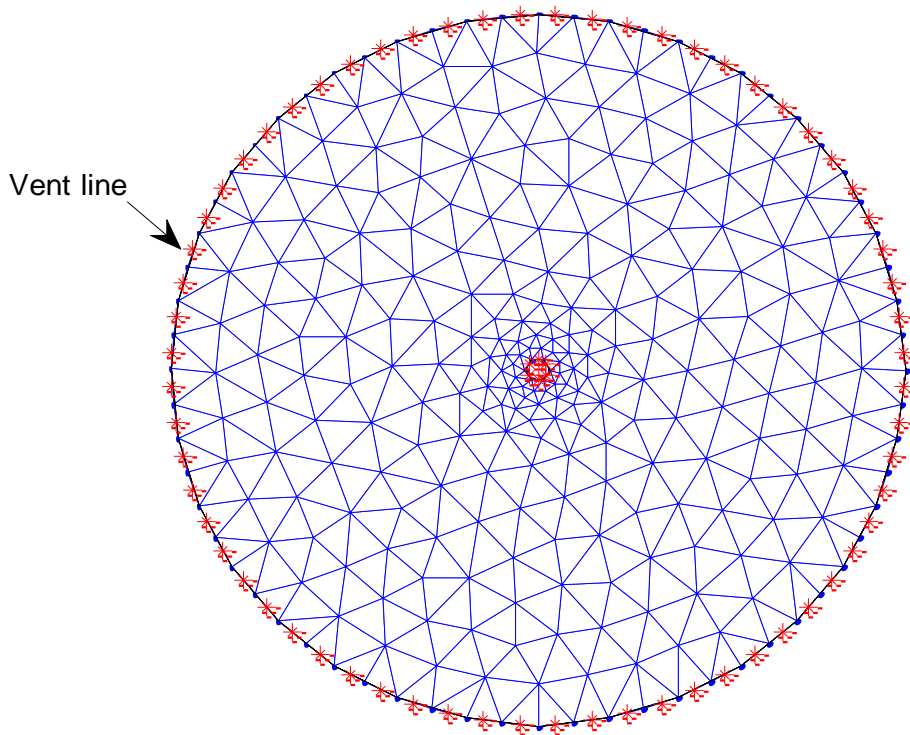
- **Curing time - Minimize**
- **Part Quality – Maximize (Through thickness temperature gradients within the part – Minimize)**



Fill phase simulation example - RTM, CRTM force evolution



Axisymmetric part centrally injected with a reactive epoxy resin.



Process variables:

Injection Pressure

Injection height

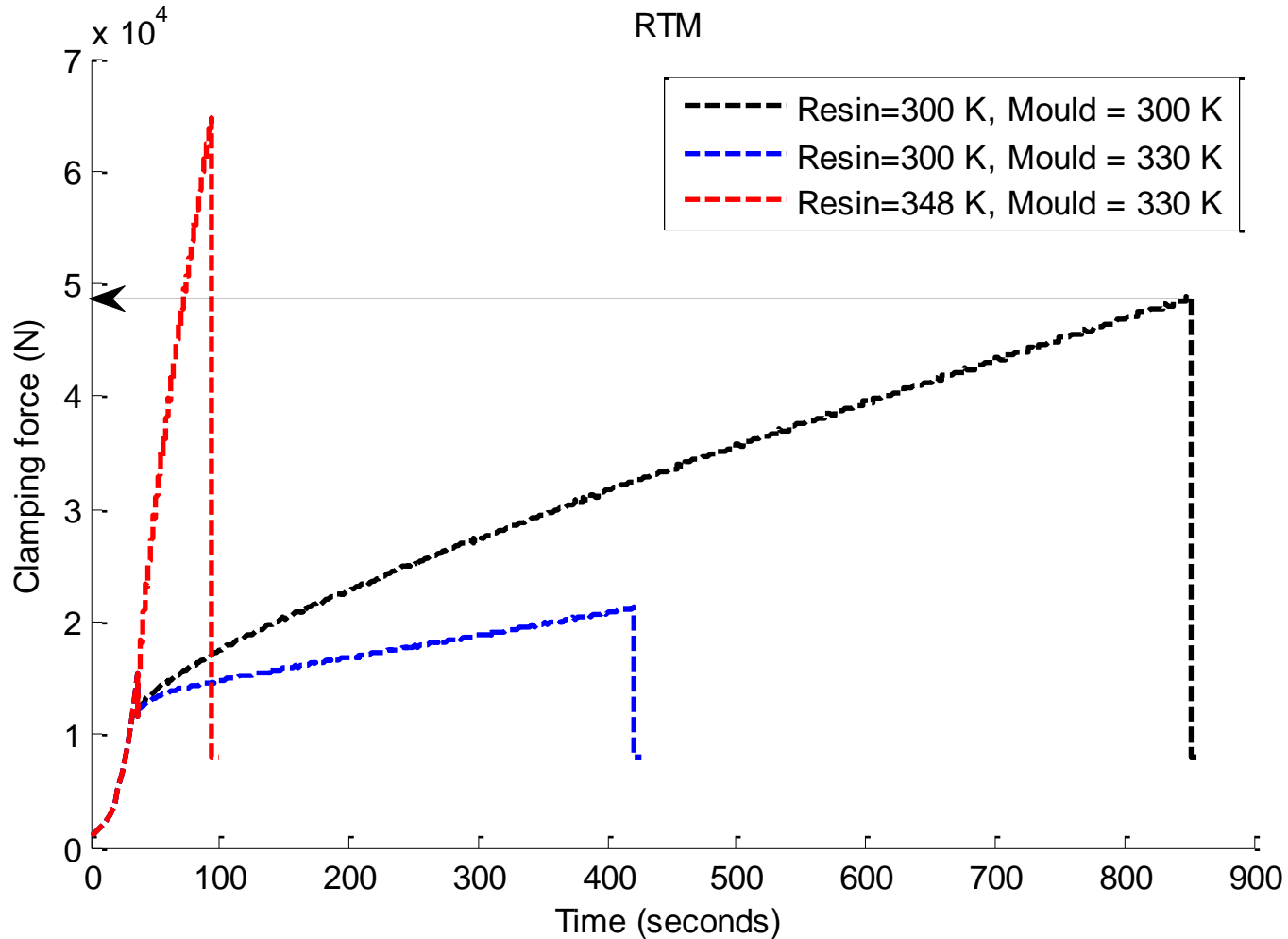
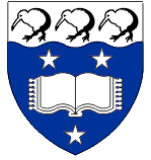
Mould closure velocity

Preheated resin temperature

Mould temperature

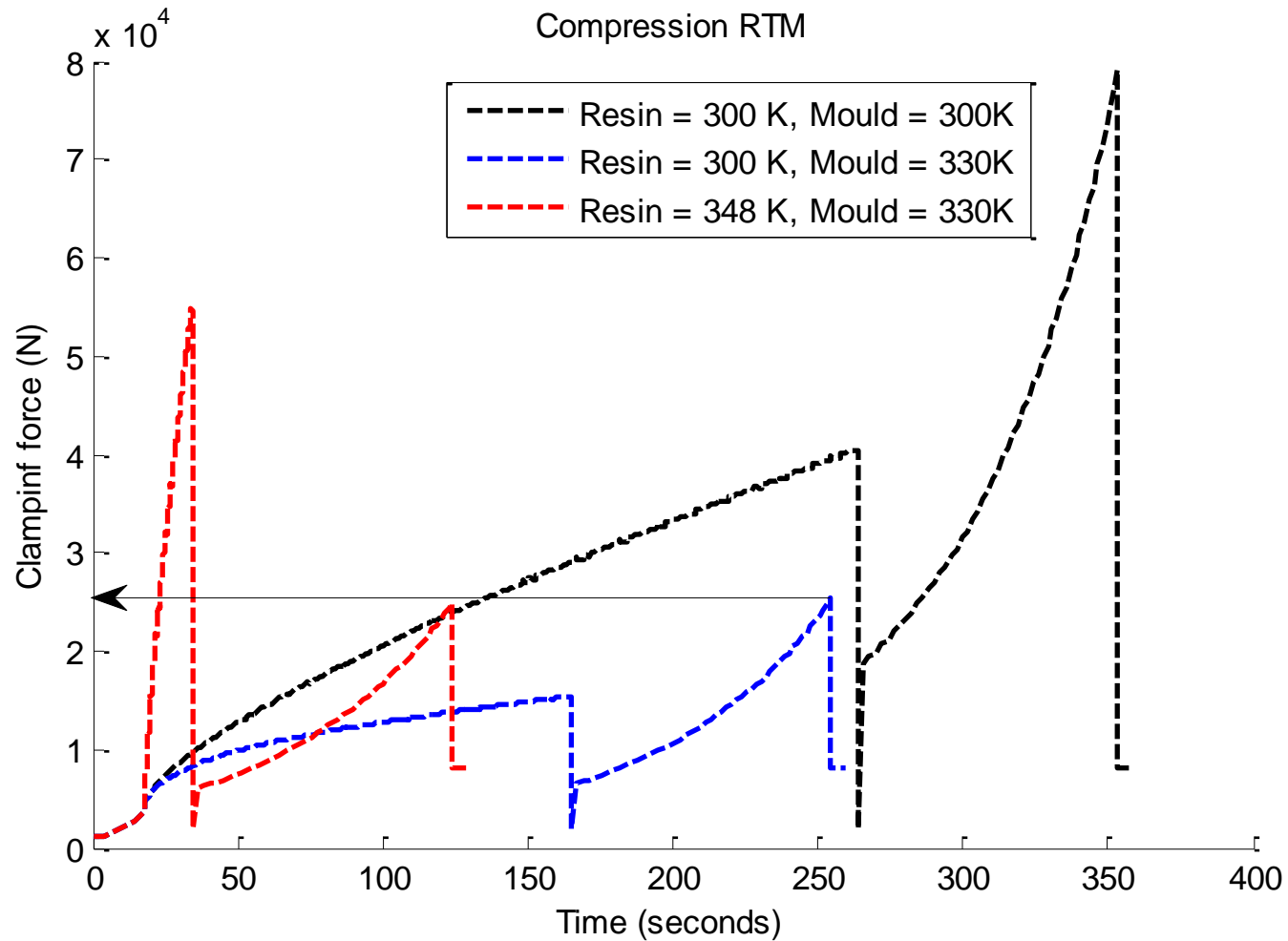
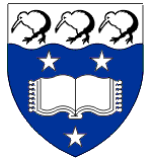


Simulation example 1 - RTM



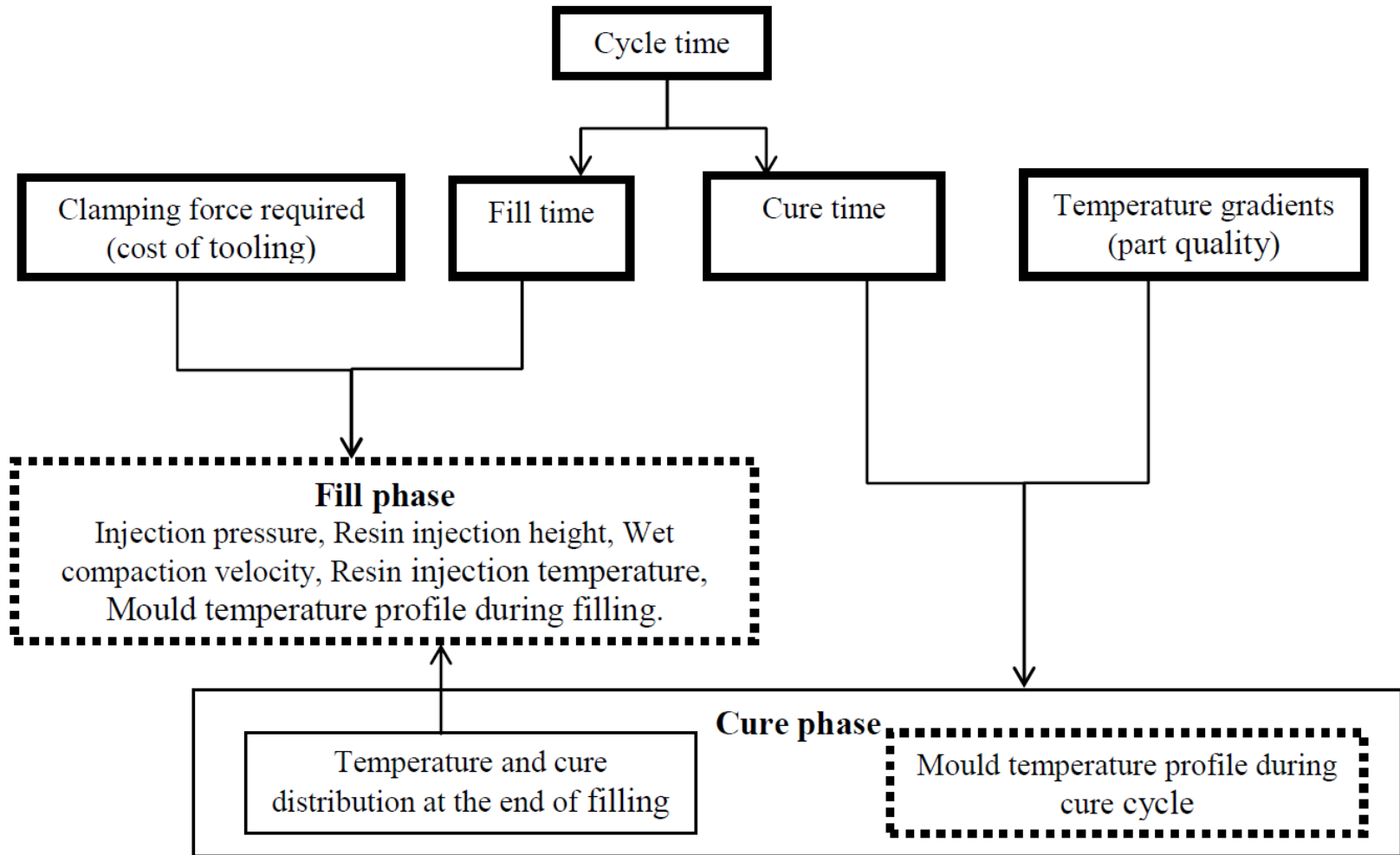
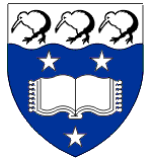


Simulation example 2 - CRTM



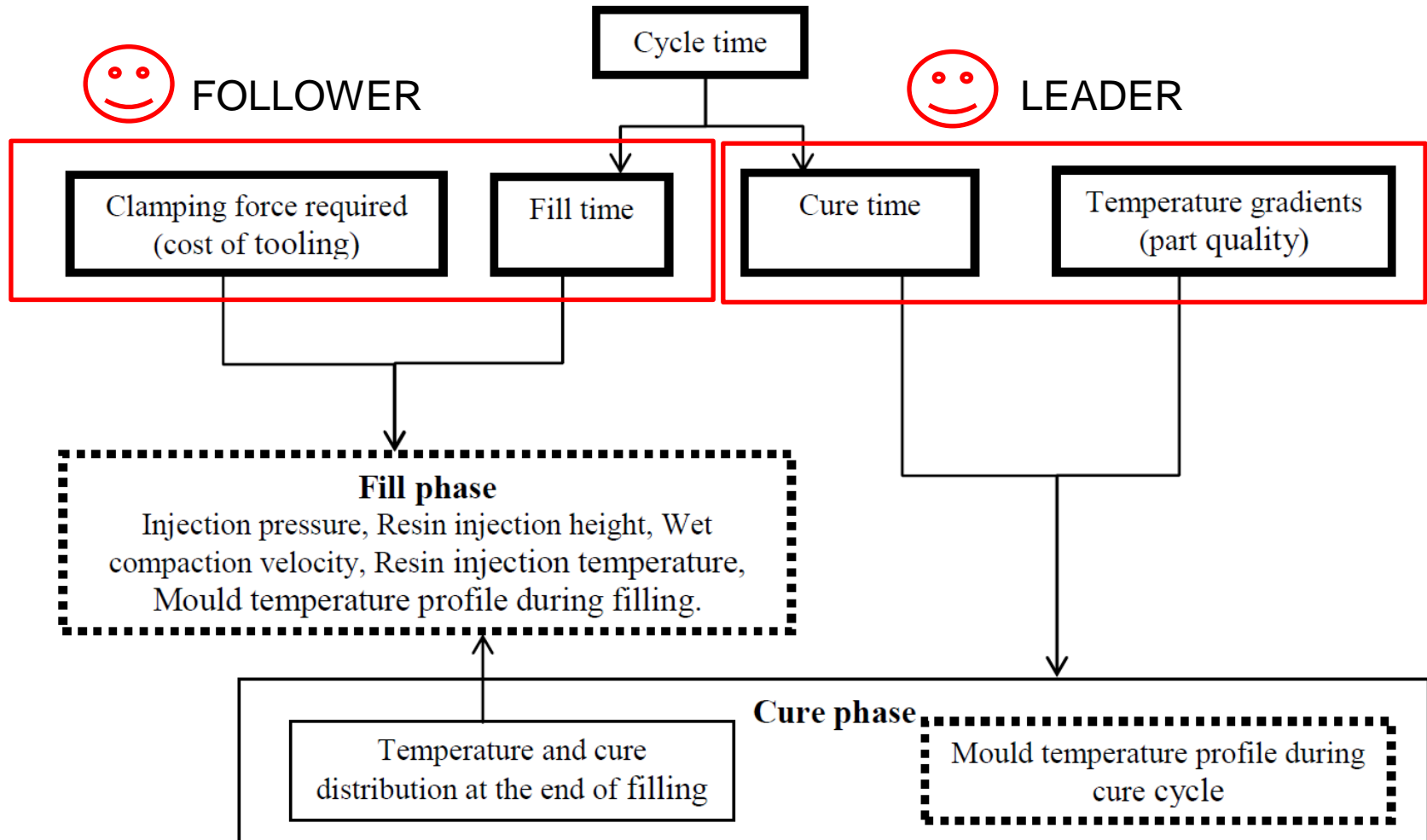
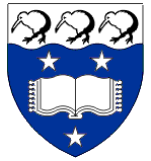


The complete optimization problem



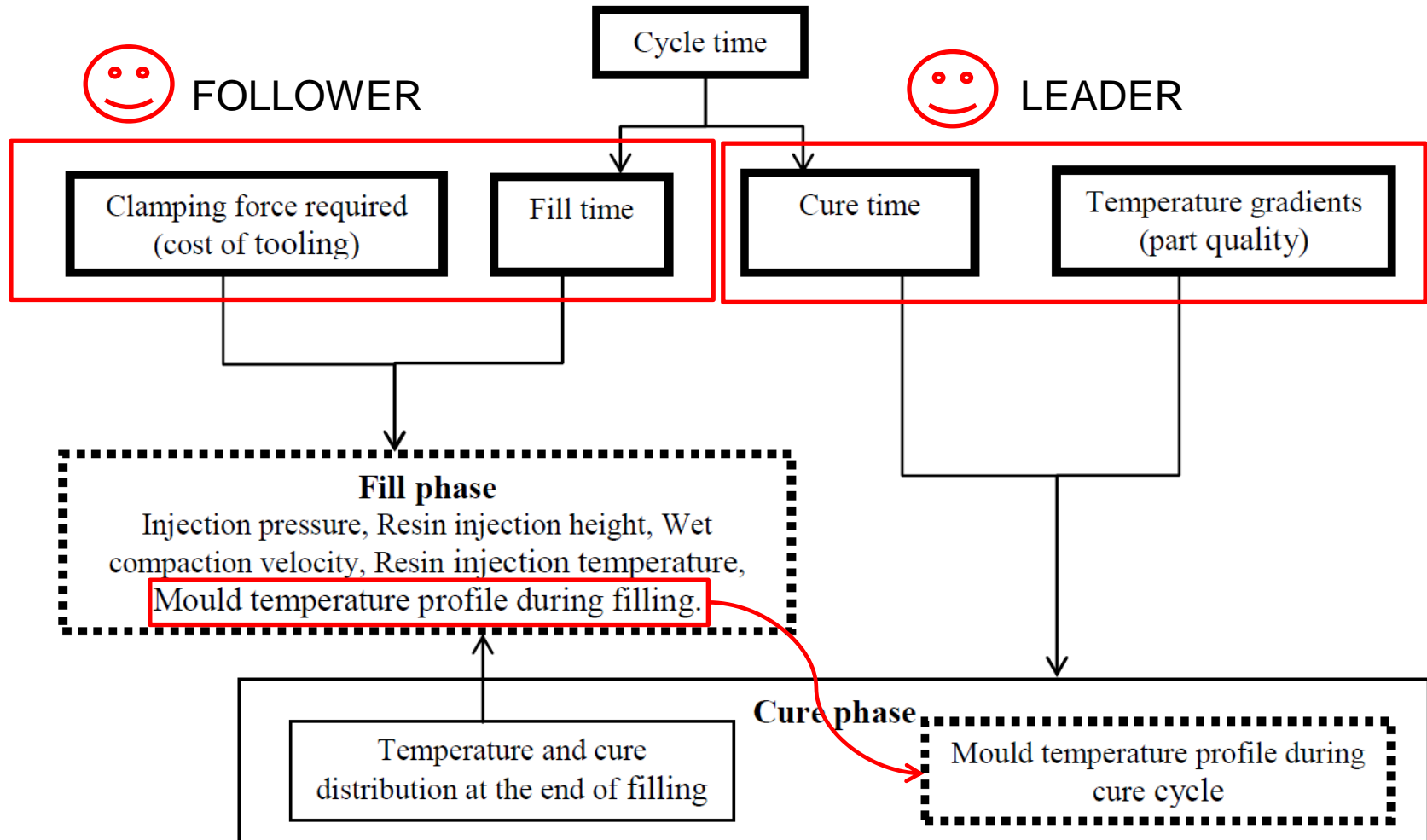
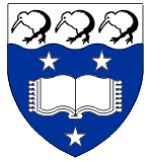


The complete optimization problem



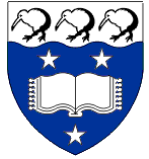


The complete optimization problem





A multi-objective Stackelberg game



General mathematical description (Optimistic approach) -

Minimize $F(x_u, x_l)$,

subject to $x_l \in \operatorname{argmin} \{f(x_l) \mid g(x_l) \geq 0, h(x_l) = 0\}$,

$G(x_u, x_l) \geq 0, H(x_u, x_l) = 0$,

$x_u = (x_1, \dots, x_r); x_l = (x_{r+1}, \dots, x_n)$,

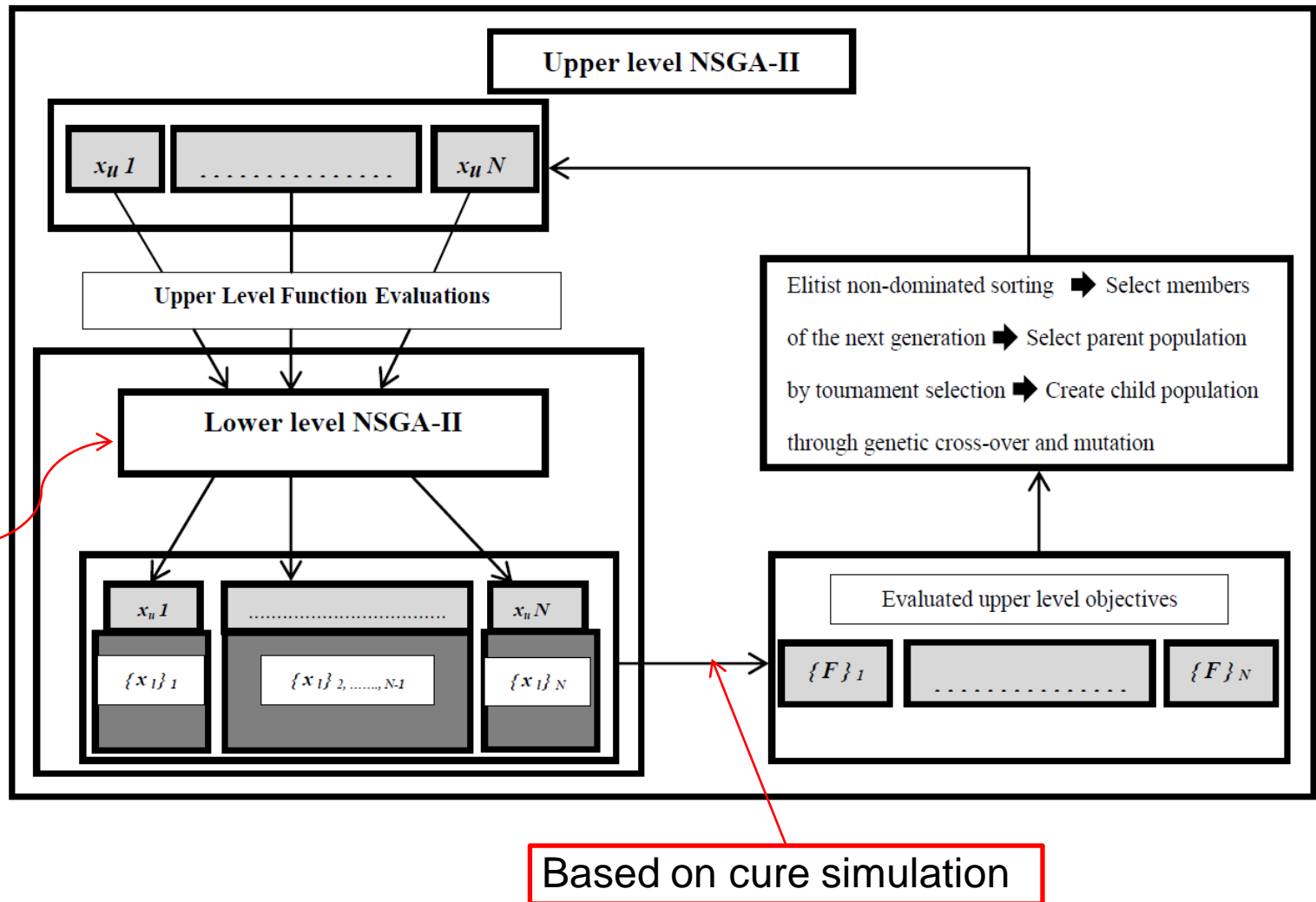
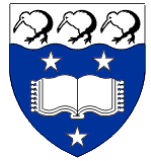
$x_i^{(L)} \leq x_i \leq x_i^{(U)}, i = 1, \dots, n$.

A slight modification (Subdued Optimism) -

$x_l \in \{\operatorname{argmin} \{f(x_l) \mid g(x_l) \geq 0, h(x_l) = 0\} \cap \{x_l: f(x_l) \in RI\}\}$

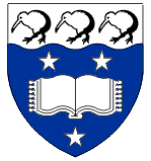


Solving the bilevel multi-objective problem





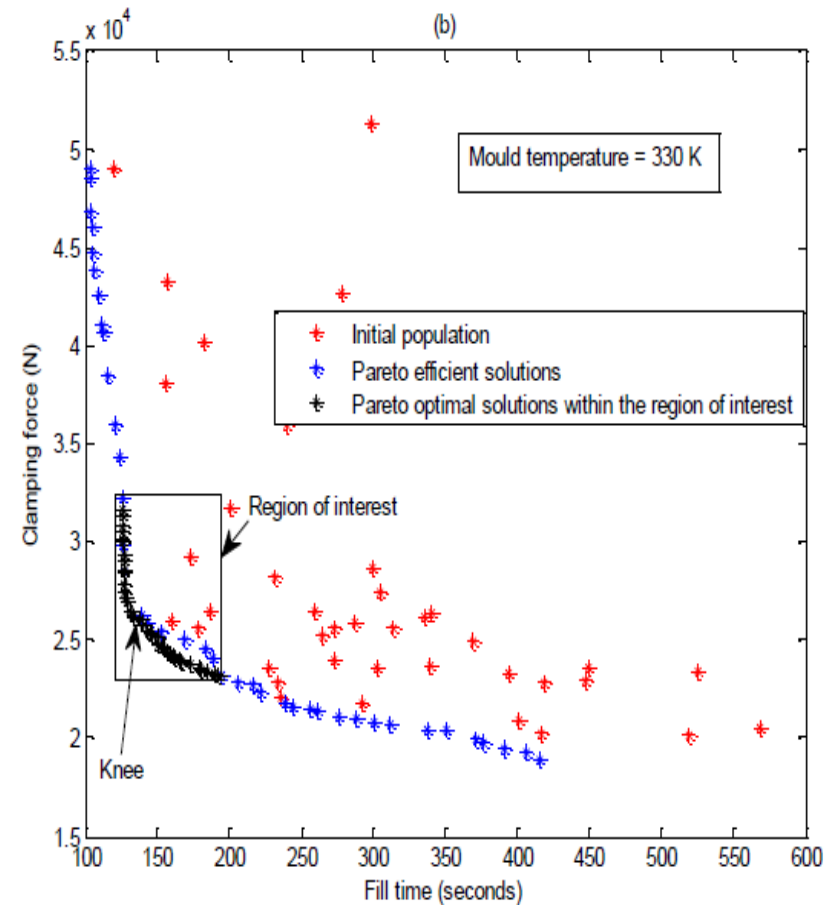
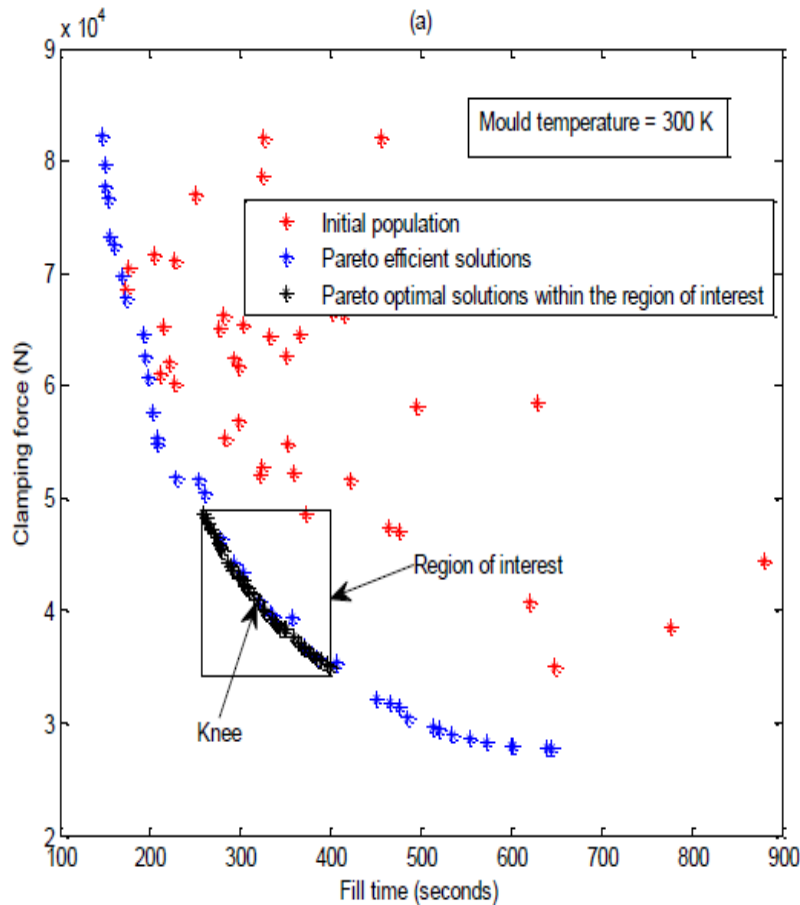
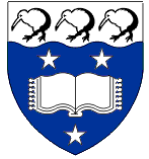
Surrogate Model



- **Simulation code is too expensive to carry out millions of lower level (fill phase) simulations.**
- **Few hundred simulations at the lower level are carried out to train a Cascade Correlation Learning Architecture neural network for subsequent function evaluations.**
- **For this a Latin Hypercube Sampling technique is used to create the reference set of points in the process variable space.**



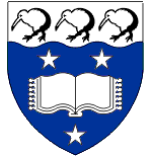
Lower-level NSGA-2 simulation



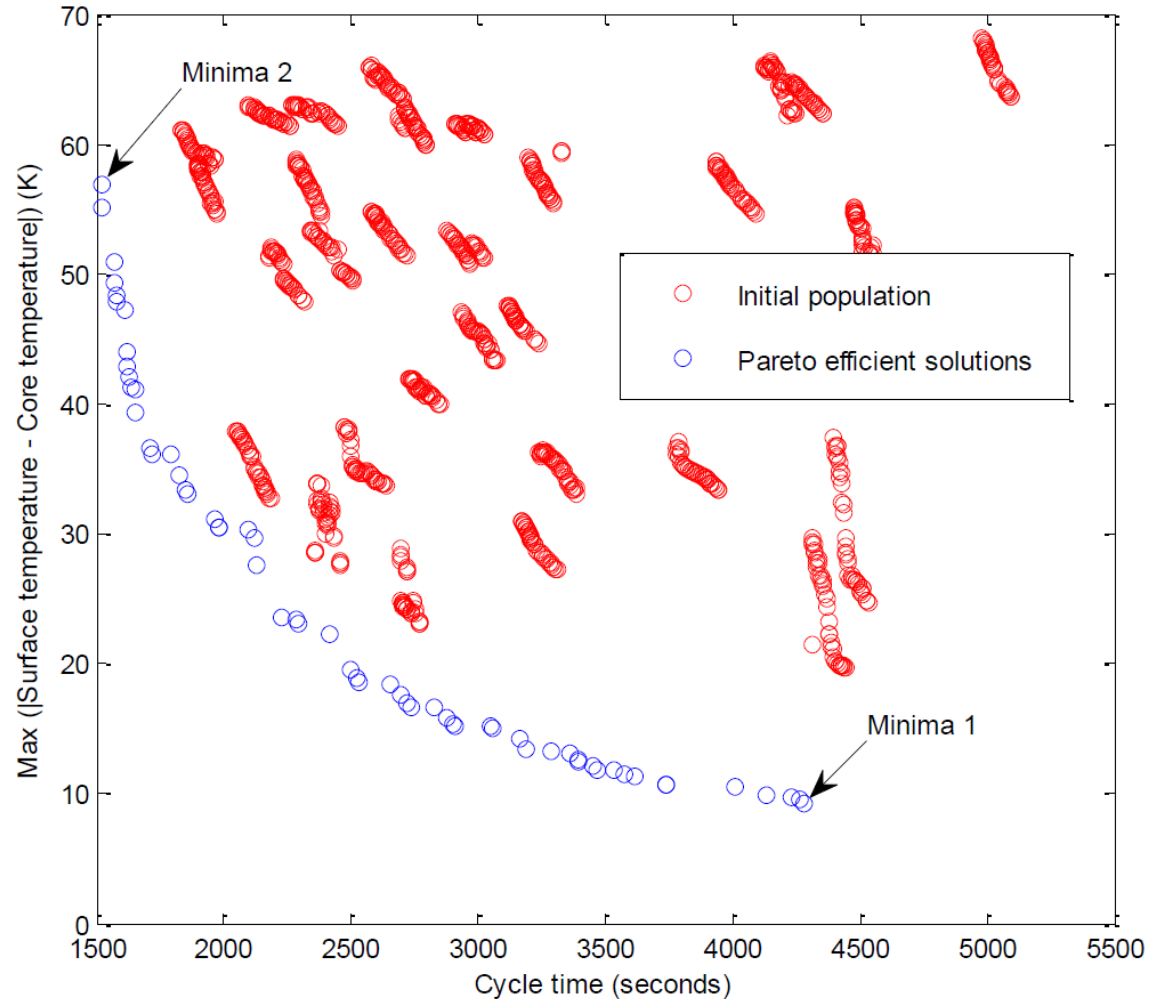
(a) Pareto frontier (blue) for a mould temperature of 300 K
(b) Pareto frontier (blue) for a mould temperature of 330 K



Overall problem solution

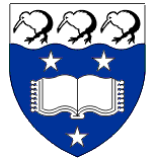


Pareto frontier obtained by the Upper Level decision maker.

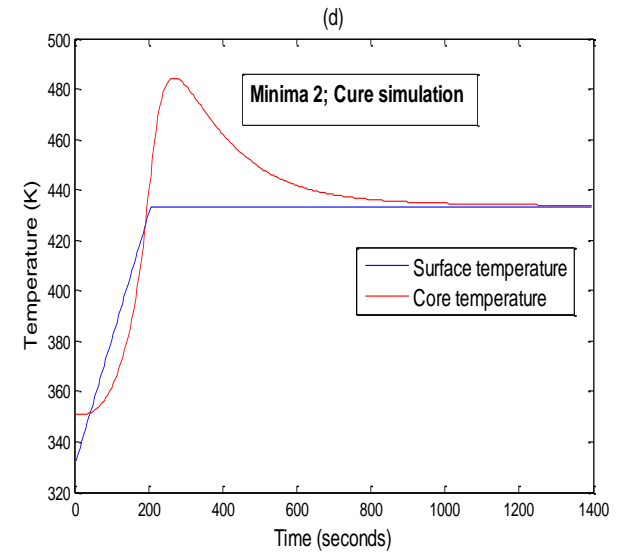
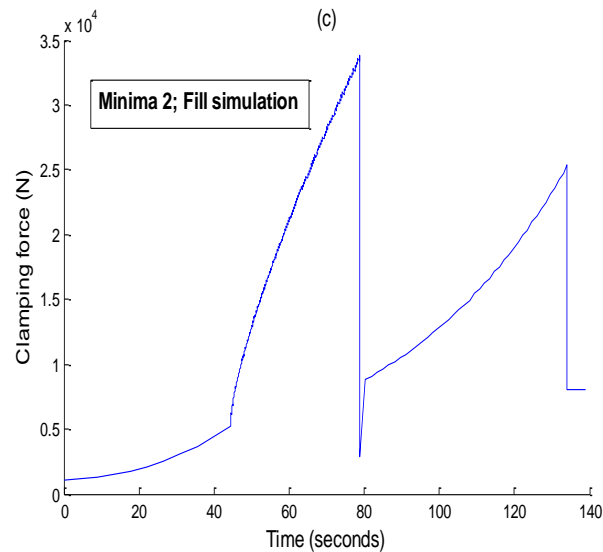
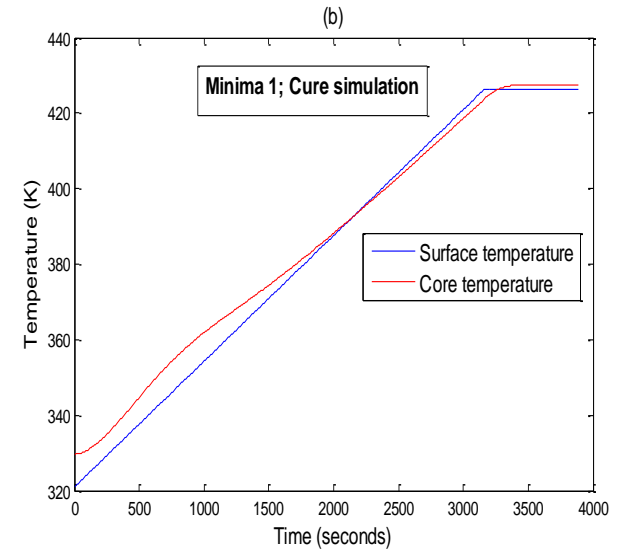
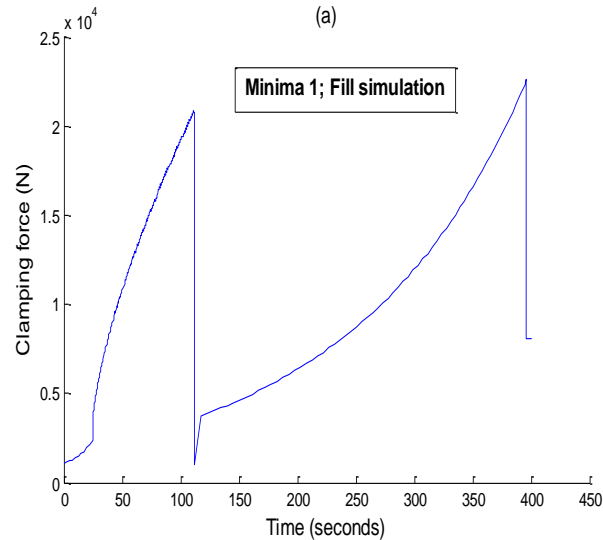




Final result analysis

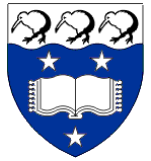


Filling and cure simulations corresponding to Minima 1 (a, b) and Minima 2 (c, d) in the previous slide



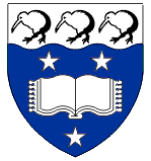


Conclusions



- **An integrated framework for optimizing the complete manufacturing cycle has been developed by using an EA based approach to solving bilevel multiobjective optimization problems.**

- **The method requires minimal interaction with the manufacturer, which is considered desirable for the problem under consideration.**



Thank You !